M-theory, Cosmological Constant and Anthropic Principle

Renata Kallosh and Andrei Linde

Department of Physics, Stanford University, Stanford, CA 94305-4060, USA (Dated: August 26, 2002)

We discuss the theory of dark energy based on maximally extended supergravity and suggest a possible anthropic explanation of the present value of the cosmological constant and of the observed ratio between dark energy and energy of matter.

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I. INTRODUCTION: ANTHROPIC CONSTRAINTS ON THE COSMOLOGICAL CONSTANT

After many desperate attempts to prove that the cosmological constant must vanish, now we face an even more complicated problem. We must understand why the cosmological constant, or the slowly changing dark energy, is at least 120 orders smaller than the Planck density M_p^4 , and, simultaneously, why its value is as large as $\Omega_D \rho_0$. Here $\rho_0 \sim 10^{-29}$ g/cm³ $\sim 10^{-120} M_p^4$ is the total density of matter in the universe at present, including the cosmological constant, or dark energy, and $\Omega_D \sim 0.7$. One of the most interesting attempts to provide such an explanation is related to anthropic principle [1].

This principle for a long time was rather controversial. It was based on an implicit assumption that the universe was created many times until the final success. It was not clear who did it and why was it necessary to make it suitable for our existence. Moreover, it would be much simpler to create proper conditions for our existence in a small vicinity of a solar system rather than in the whole universe.

These problems were resolved with the invention of inflationary cosmology. First of all, inflationary universe itself, without any external intervention, may produce exponentially large domains with all possible laws of low-energy physics [2]. And if the conditions suitable for our existence are established near the solar system, inflation ensures that similar conditions appear everywhere within the observable part of the universe. In addition to considering a single inflationary universe consisting of many domains with different values of constants, one may also consider a possibility that the inflationary universe may be born in many different quantum states with different values of coupling constants, see e.g. [3, 4, 5, 6]. This provides a simple justification of the cosmological anthropic principle and allows one to apply it to the cosmological constant problem.

If, for example, the cosmological constant is large and negative, $\Lambda \ll -10^{-29}$ g/cm³, then such a universe, even if it is flat, would collapse within the time that is smaller than the age of our universe $t \sim 14$ billion years [1, 7]. This would make our life impossible. One may wonder whether intelligent life could emerge within 7 billion years or 5 billion years, but we have no reason to believe that it could happen on a much shorter time scale.



FIG. 1: Evolution of a flat Λ CDM universe for various values of Λ . Time is in units of the present age of the universe $t_0 \approx 14$ billion years. The present moment is placed at t = 0, the big bang corresponds to t = -1. The upper (red) line corresponds to the flat universe with $\Omega_{\text{tot}} = 1$, $\Omega_{\Lambda} = 0.7$ (i.e. $\Lambda = +0.7\rho_0$) and $\Omega_M = 0.3$. The next line below it (the blue line) corresponds to a flat universe with $\Lambda = -4.7\rho_0$. As we see, this universe collapses at the age of 14 billion years. The total lifetime of the universe with $\Lambda = -18.8\rho_0$ (the lower, green line) is only 7 billion years.

Since we are entering the age of precision cosmology, let us improve the order-of-magnitude estimates of [1, 7] and obtain a numerical constraint on negative Λ . The investigation is straightforward, so we will simply show the results in Fig. 1. We find that the anthropic constraint on the negative cosmological constant is a bit less stringent than it was anticipated. If 7 billion years is sufficient for emergence of human life, then $\Lambda \gtrsim -18.8\rho_0 \sim -2 \times 10^{-28}$ g/cm³. If we really need about 14 billion years, as one can infer from [8], then the constraint is somewhat stronger: $\Lambda \gtrsim -4.7\rho_0 \sim -5 \times 10^{-29}$ g/cm³.

However, the present observational data suggest that $\Lambda > 0$. In this case the use of the anthropic considerations become more involved. In [7] it was argued that the life of our type is impossible for $\Lambda \gg 10^{-29}$ g/cm^3 because in this case the density of matter of the universe would be exponentially small due to its exponential expansion at the present stage. A more precise and rigorous constraint was obtained later by Weinberg [9]. He pointed out that the process of galaxy formation occurs only up to the moment when the cosmological constant begins to dominate the energy density of the universe and the universe enters the stage of late-time inflation. (By galaxy formation we understand the growth of density contrast until the moment when the galaxy separates from the general cosmological expansion of the universe. After that, its density rapidly grows by a factor of $O(10^2)$, and its subsequent evolution becomes much less sensitive to the value of Λ .) For example, one may consider galaxies formed at $z \gtrsim 4$, when the energy density of the universe was 2 orders of magnitude greater than it is now. Such galaxies would not form if $\Lambda \gtrsim 10^2 \rho_0 \sim 10^{-27} \text{ g/cm}^3$.

Thus, anthropic considerations may reduce the disagreement between the theoretical expectations $(\Lambda \sim M_p^4)$ and observational data $(\Lambda \sim \rho_0 \sim 10^{-120} M_p^4)$ from 120 orders of magnitude to only 2 orders of magnitude! But this is not yet a complete solution of the cosmological constant problem. Assuming that all values of the cosmological constant are equally probable, one would find himself in a universe with $\Lambda \sim \rho_0$ with the probability about 1%.

The next important step was made in [10, 11, 12,13, 14]. The authors considered not only our own galaxy, but all other galaxies that could harbor life of our type. This would include not only the existing galaxies but also the galaxies that are being formed at the present epoch. Since the energy density al later stages of the evolution of the universe becomes smaller, even a very small cosmological constant may disrupt the late-time galaxy formation, or may prevent the growth of existing galaxies. This allowed the authors of [10, 11, 12, 13, 14] to strengthen the constraint on the cosmological constant. According to [12], the probability that an astronomer in any of the universes would find a value of $\Omega_D = \Lambda/\rho_0$ as small as 0.7 ranges from 5% to 12%, depending on various assumptions.

However, our goal is not to find suitable conditions for the human life in general, but rather to explain the results of our observations. These results include the fact that for whatever reason we live in an internal part of the galaxy that probably could not be strongly affected by the existence of a cosmological constant $\Lambda \sim \rho_0$. Does it mean that we are not typical observers since we live in an atypical part of the universe where we are protected against a small cosmological constant $\Lambda \sim \rho_0$? Also, galaxy formation is not a one-step process. The central part of our galaxy was formed very early, at $z \gtrsim 20$, when the energy density in the universe was 4 orders of magnitude greater than it is now. To prevent formation of such regions one would need to have $\Lambda \gtrsim 10^4 \rho_0 \sim 10^{-25} \text{ g/cm}^3$. It may happen that the probability of emergence of life in such regions, or in the early formed dwarf galaxies, is very small. Moreover, one could argue that the probability of emergence of life is proportional to the fraction of matter condensed into large galaxies [10, 11, 12, 13, 14]. Even if it is so, in an eternally existing inflationary universe there should be indefinitely many regions suitable for existence of life, so life would eventually appear in one of such places even if the probability of such event is extremely small. A more detailed investigation of this issue is in order [15].

In this respect the anthropic constraint on $\Lambda < 0$ seems to be less ambiguous. But it is also less important since it does not seem to apply to an accelerating universe with $\Lambda \approx 0.7\rho_0$. In this paper we will show, however, that a similar constraint based on investigation of the total lifetime of a flat universe can be derived in a broad class of theories based on N=8 supergravity that can describe the present stage of acceleration [16, 17, 18, 19]. This may allow us to avoid fine-tuning that is usually required to explain the observed value of Ω_D .

II. MAXIMAL SUPERGRAVITY AS DARK ENERGY HIDDEN SECTOR

Usually in all discussions of the cosmological constant in the astrophysical literature it is assumed that one can simply add a cosmological constant term describing vacuum energy to the gravitational Lagrangian. However, it appears to be extremely difficult to do so in the context of M/string theory.

All known compactifications of the fundamental M/string theory to four dimensions do not lead to potentials with de Sitter solutions corresponding to $\Lambda > 0$. However, there are versions of the maximally extended d = 4 N = 8 supergravity which have dS solutions. They are also known to be solutions of d = 11 supergravity with 32 supersymmetries, corresponding to M/string theory [20]. dS_4 solutions of d = 4 N = 8 supergravity correspond to solutions of M/string theory with non-compact internal seven (six) dimensional space. The relation between states of higher dimensional and four dimensional theory in

such backgrounds is complicated since the standard Kaluza-Klein procedure is not valid in this context. It is nevertheless true that the class of d = 4 supergravities with dS solutions that we will consider below as dark energy candidates has a direct link to M/string theory, as opposite to practically any other model of dark energy. Moreover, these theories with maximal amount of supersymmetries are perfectly consistent from the point of view of the d = 4 theory: all kinetic terms for scalars and vectors are positive definite.

All supersymmetries are spontaneously broken for dS solutions of N = 8 supergravity. These dS solutions are unstable; they correspond either to a maximum of the potential for the scalar fields ϕ or to a saddle point. In all known cases one finds [16] that there is a tachyon and the ratio between $V'' = m^2$ and $\Lambda = V$ at the extremum of $V(\phi)$ is equal to -2.

According to current cosmological data, the relevant dS_4 space is defined as a hypersurface in a 5d space $-T^2 + (X^2 + Y^2 + Z^2 + W^2) = H_0^{-2}$. Here H_0 is the Hubble parameter. Its inverse, H_0^{-1} , determines time scale of the same order as the age of the universe, $H_0^{-1} \sim 10^{10}$ years. One of the simplest solutions of d = 11 supergravity is given by a warped product of a four-dimensional dS space and a seven-dimensional hyperboloid $H^{p,q}$. A fiducial model where all scalars are constant is defined by dS surface presented above and the surface in an eight-dimensional space defining an internal space hyperboloid $H^{p,q}$. This surface is given by $\eta_{AB} z^A z^B = \alpha H_0^{-2}$, where the constant α depends on p, q and the metric η_{AB} is constant and has p positive eigenvalues and q negative eigenvalues and p + q = 8.

A simplest (and typical) representative of d = 4N = 8 supergravities with dS maximum, originated from M-theory, has the following action [21]:

$$g^{-1/2}L = -\frac{1}{2}R - \frac{1}{2}(\partial\phi)^2 - \Lambda(2 - \cosh\sqrt{2}\phi) \ . \tag{1}$$

Here we use units $M_p = 1$. At the critical point V' = 0, $V_{cr} = \Lambda$, $\phi_{cr} = 0$.

This corresponds to the case p = q = 4 and d = 4supergravity has gauged SO(4, 4) non-compact group. At dS vacuum it is broken down to its compact subgroup, $SO(4) \times SO(4)$. The value of the cosmological constant Λ is related to H_0 and to the gauge coupling q as follows:

$$\Lambda = 3H_0^2 = 2g^2 \; .$$

A similar potential was obtained in N=4 gauged supergravity in [22], where dS solution of extended supergravity was found for the first time and where it was pointed out that it is unstable, being a maximum of the potential.

The gauge coupling and the cosmological constant in d = 4 supergravity have the same origin in Mtheory: they come from the flux of an antisymmetric 0.5

FIG. 2: Scalar potential $V(\phi) = \Lambda(2 - \cosh\sqrt{2}\phi)$ in d = 4 N = 8 supergravity (1). The value of the potential is shown in units of Λ , the field is given in units of M_p .

0.2

-0.2

-0.4

-0.5

tensor gauge field strength [20]. The corresponding 4-form $F_{\mu\nu\lambda\rho}$ in d = 11 supergravity is proportional to the volume form of the dS_4 space:

$$F_{0123} \sim \sqrt{\Lambda} V_{0123}$$
 . (2)

Here F = dA where A is a 3-form potential of d = 11supergravity. According to this model, the small value of the cosmological constant is due to the 4-form flux which has the inverse time-scale of the order of the age of the universe. Note that in our model there is no reason for the flux quantization since the internal space is not compact. This makes it different from [23] where the flux and/or its changes were quantized. The eleven-dimensional origin of the scalar field ϕ in the potential can be explained as follows. Directly in d=4 N = 8 gauged supergravity has 35 scalars and 35 pseudo-scalars, forming together a coset space $\frac{E_{7(7)}}{SU(8)}$. The field ϕ is an $SO(4) \times SO(4)$ invariant combination of these scalars and it may also be viewed as part of the d = 11 metric.

The first idea would be to discard this model altogether because its potential is unbounded from below. However, the scalar potential in this theory remains positive for $|\phi| \leq 1$, and for small Λ the time of development of the instability can be much greater than the present age of the universe, which is quite sufficient for our purposes [16, 17, 18, 19]. In fact, we will see that this instability allows us to avoid the standard fine-tuning/coincidence problem plaguing most of the versions of the theory of quintessence. To use these theories to describe the present stage of acceleration (late inflation) one should take $\Lambda \sim 10^{-120} M_p^4$. This implies that the tachyonic mass is ultra-light, $|m^2| \sim -(10^{-33} \text{ eV})^2$.

In the early universe the ultra-light scalar fields may stay away from the extrema of their potentials; they 'sit and wait' and they begin moving only when the

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Hubble constant decreases and becomes comparable with the scale of the scalar mass. This may result in noticeable changes of the effective cosmological constant during the last few billion years.

Since the potential of N = 8 supergravity with dS solution is unbounded from below, the universe will eventually collapse. If the initial position of the field is not far from the top of the potential, the time before the collapse may be very long [19].

From the perspective of the d = 11 theory it is natural to consider a large ensemble of possible values for the fields $F \sim \sqrt{\Lambda}$ and ϕ and study it. In the context of the d = 4 theory one may also study a large ensemble of values for Λ and ϕ .

III. ANTHROPIC CONSTRAINTS ON THE COSMOLOGICAL CONSTANT IN N=8 SUPERGRAVITY

Consider a theory of a scalar field ϕ with the effective potential $V(\phi) = \Lambda(2 - \cosh\sqrt{2}\phi)$ in the N = 8theory (1). In order to understand the cosmological consequences of this theory, let us first consider this potential at $|\phi| \ll 1$. In this limit the potential has a very simple form,

$$V(\phi) = \Lambda(1 - \phi^2) = 3H_0^2(1 - \phi^2) .$$
 (3)

The main property of this potential is that $m^2 = V''(0) = -2\Lambda = -6H_0^2$. One can show that a homogeneous field $\phi \ll 1$ with $m^2 = -6H_0^2$ in the universe with the Hubble constant H_0 grows as follows: $\phi(t) = \phi_0 \exp cH_0 t$, where $c = (\sqrt{33} - 3)/2 \approx 1.4$. Consequently, in the universe with the energy density dominated by $V(\phi)$ it takes time $t \sim 0.7H_0^{-1} \ln \phi_0^{-1}$ until the scalar field rolls down from ϕ_0 to the region $\phi \gg 1$, where $V(\phi)$ becomes negative and the universe collapses.

This means that one cannot take large Λ without making the total lifetime of the universe too short to support life, unless the scalar field ϕ_0 was exponentially small. But if the potential of the field ϕ always was very flat, then one can assume that the field ϕ initially (or after inflation) can take any value ϕ_0 with equal probability, so there is no reason to expect that ϕ_0 must be very small. This means that for $\phi_0 \leq 1$ the typical lifetime of the universe is $t_{\text{tot}} \sim H_0^{-1} \sim \Lambda^{-1/2}$. Therefore the universe can live longer than 14 billion years only if the cosmological constant is extremely small, $\Lambda \leq \rho_0$.

On the other hand, for $\phi \gg 1$ the potential falls down exponentially, $V(\phi) \sim -\Lambda \exp \sqrt{2}|\phi|$. Therefore for $\phi \gg 1$ the universe almost instantly collapses even if $\Lambda \lesssim \rho_0$.

Now we can study this process numerically, solving a system of equations for the scale factor a(t) and the scalar field $\phi(t)$.

$$\ddot{\phi} + 3\frac{\dot{a}}{a}\dot{\phi} - V'(\phi) = 0 ,$$

$$\frac{\ddot{a}}{a} = \frac{V - \dot{\phi}^2 - \rho_M}{3} ,$$

where $\rho_M = C/a^3(t)$, and $\phi'_0 = 0$. A detailed description of our approach can be found in [19]. Here we will present some of our results related to the cosmological constant problem.

Fig. 3 shows expansion of the universe for $\phi_0 = 0.25$, and for various values of Λ ranging from $0.7\rho_0$ to $700\rho_0$. Time is given in units of 14 billion years. One finds, as expected, that the total lifetime of the universe for a given ϕ_0 is proportional to $\Lambda^{-1/2}$, which means that large Λ are anthropically forbidden.



FIG. 3: Expansion of the universe for $\phi_0 = 0.25$. Going from right to left, the first (red) line corresponds to $\Lambda = 0.07\rho_0$, the second (green) line corresponds to $\Lambda = 0.7\rho_0$, then $\Lambda = 7\rho_0$, $70\rho_0$ and $700\rho_0$.

Fig. 4 shows expansion of the universe for $\Lambda = 0.7\rho_0$. The upper (red) line corresponds to the fiducial model with $\phi_0 = 0$. In this case the field does not move and all cosmological consequences are the same as in the standard theory with the cosmological constant $\Lambda = 0.7\rho_0$. The difference will appear only in a very distant future, at $t \sim 10^2 H_0^{-1} \sim 10^3$ billion years, when the unstable state $\phi_0 = 0$ will decay due to the destabilizing effect of quantum fluctuations [16]. For $\phi_0 > 1$ the total lifetime of the universe becomes unacceptably small, which means that large ϕ_0 are anthropically forbidden.

Further conclusions will depend on various assumptions about the probability of parameters (Λ, ϕ_0) . In this section we will make the simplest assumption that all values of Λ and ϕ_0 are equally probable. We will discuss alternative assumptions and their consequences in the next section.

All possible values of Λ and ϕ_0 corresponding to the total lifetime of the universe greater than 14 billion



FIG. 4: Expansion of the universe for $\Lambda = 0.7\rho_0$. The upper (red) line corresponds to the fiducial model with $\phi_0 = 0$ (cosmological constant; field does not move). The (green) line below corresponds to $\phi = 0.5$. The next (blue) line corresponds to $\phi = 1$, then to $\phi = 1.5$, and $\phi = 2$.

years are shown in Fig. 5, in the region under the thick (red) line. If all values of Λ and ϕ_0 are equally probable, the measure of probability is given by the area. The total area under the curve is finite, $S_{\text{tot}} \approx 3.5$. One can easily estimate the probability to be in any region of the phase space (Λ, ϕ_0) by measuring the corresponding area and dividing it by S_{tot} .



FIG. 5: The region below the thick (red) line contains all possible Λ and ϕ_0 corresponding to the total lifetime of the universe greater than 14 billion years. The dashed line $\Lambda \approx 1.5\rho_0$ separates this region into two equal area parts. The region below the thin (blue) curve corresponds to all universes with the lifetime greater than 28 billion years, i.e. to the universes that would live longer than 14 billion years after the present moment.

The dashed line $\Lambda \approx 1.5\rho_0$ separates the anthropically allowed region into two equal area parts. This implies that the average value of Λ in this theory is about $1.5\rho_0$. It is obvious that Λ can be somewhat larger or somewhat smaller than $1.5\rho_0$, but the main part of the anthropically allowed area corresponds to

$$\Lambda = O(\rho_0) \sim 10^{-120} M_p^4$$

This is one of the main results of our investigation. This result is a direct consequence of the relation $m^2 = -6H_0^2$ which is valid for all known versions of d = 4 N = 8 supergravity that allow dS solutions.

The region below the thin (blue) curve corresponds to all universes with the lifetime greater than 28 billion years, i.e. to the universes that would live longer than 14 billion years after the present moment. The area below this curve is 3 times smaller than the area between the thin (blue) curve and the thick (red) curve. This means that the "life expectancy" of a typical anthropically allowed universe (the time from the present moment until the global collapse) is smaller than the present age of the universe. The prognosis becomes a bit more optimistic if one takes into account that we live in the universe with $\Omega_D = 0.7$: The probability that the universe will survive more than 14 billion years from now becomes better than 50%.

Finding the average value of Λ does not immediately tell us what is the most probable value of Ω_D . In order to do it we plot in Fig. 6 the curves corresponding to $\Omega_D = 0.5$ (blue line, just below the thick red line), $\Omega_D = 0.7$ (green line, just below the line $\Omega_D = 0.5$), and $\Omega_D = 0.9$ (pink line, below the line $\Omega_D = 0.7$). The region to the left of the thin dashed line corresponds to the universes that accelerate at the present time (14 billion years after the big bang).



FIG. 6: The curves corresponding to $\Omega_D = 0.5$ (blue line below the thick red line), $\Omega_D = 0.7$ (green line), and $\Omega_D =$ 0.9 (pink line). The region to the right of the thin dashed line corresponds to the universes that accelerate 14 billion years after the big bang.

The total probability to live in an accelerating universe at the time 14 billion years after the big bang is determined by the area bounded by the thin dashed line in Fig. 6. Dividing this area by $S_{\rm tot} \approx 3.5$, one can find that this probability is about 35%. About a half of this area corresponds to $\Omega_d > 0.9$. The most interesting part of the accelerating region is bounded by the blue curve $\Omega_D = 0.5$, the pink curve $\Omega_D = 0.9$ and the thin dashed line. All points inside this region correspond to accelerating universes with $0.5 < \Omega_D < 0.9$. As one can easily see from Fig. 6, the area of the anthropically allowed region $S_{\rm tot} \approx 3.5$ one finds that the probability to live in such a universe is about 10%. These results resolve the fine-tuning/coincidence problem in the theory of dark energy.

IV. DISCUSSION

Most of the theories of dark energy have to face two problems. First of all, it is necessary to explain why does the bare cosmological constant vanish. Then one must find a dynamical mechanism imitating a small cosmological constant and explain why $\Omega_D \sim 0.7$ at the present stage of the evolution of the universe.

In this paper we studied cosmological consequences of the simplest toy model of dark energy based on N = 8 supergravity. We have found that in the context of this theory one can completely resolve the cosmological constant problem, as well as the coincidence problem plaguing most models of quintessence.

Indeed, one simply cannot add a cosmological constant to this theory. The only way to introduce something similar to the cosmological constant is to put the system close to the top of the effective potential. If the potential is very high, then it is also very curved, V''(0) = -2V(0). We have found that the universe can live long enough only if the field ϕ initially is within the Planck distance from the top, $|\phi| \leq M_p$, which sounds reasonable, and if V(0), which plays the role of Λ in this theory, does not exceed much the critical value $\rho_0 \sim 10^{-120} M_p^4$.

In our paper we made the simplest assumption that the probability to live in the universe with different Λ and ϕ_0 does not depend on their values. However, in realistic models the situation may be different. For example, as we mentioned, $\Lambda^{1/2}$ is related to the 4form flux in d = 11 supergravity, see Eq. (2). This may suggest that the probability distribution should be uniform not with respect to Λ and ϕ_0 but with respect to $\Lambda^{1/2}$ and ϕ_0 . We studied this possibility and found that the numerical results change, but the qualitative features of the model remain the same.

The probability distribution for ϕ_0 also may depend on ϕ_0 even if $V(\phi)$ is very flat at $\phi < 1$. First of all, it might happen that the fields $\phi \gg 1$ (i.e. $\phi \gg M_p$) are forbidden, or the effective potential at large ϕ blows up. This is often the case in N = 1 supergravity. Secondly, interactions with other fields in the early universe may create a deep minimum capturing the field ϕ at some time-dependent point $\phi < 1$. This also often happens in N = 1 supergravity, which constitutes one of the features related to the cosmological moduli problem. If this happens in our model, one will be able to ignore the region of $\phi_0 > 1$ (the right part of Figs. 5, 6) in the calculation of probabilities. This will increase the probability to live in an accelerating universe with $0.5 < \Omega_D < 0.9$.

In our estimates we assumed that the universe must live as long as 14 billion years before the human life appears. One could argue that the first stars and planets were formed long ago, so we may not need much more than about 5-7 billion years for the development of life. This would somewhat decrease our estimate for the probability to live in an accelerating universe with $0.5 < \Omega_D < 0.9$, but this would not alter our results qualitatively. On the other hand, most of the planets were probably formed at later stages of the evolution of the universe [8], so one may argue that the probability of emergence of human life becomes much greater at t > 14 billion years, especially if one keeps in mind how many coincidences have made our life possible. If one assumes that human life is extremely improbable (after all, we do not have any indications of its existence anywhere else in the universe), then one may argue that the probability of emergence of life becomes significant only if the total lifetime of the universe can be much greater than 14 billion years. This would increase our estimate for the probability to live in an accelerating universe with $0.5 < \Omega_D < 0.9$.

So far we did not use any considerations based on the theory of galaxy formation [9, 10, 11, 12, 13, 14]. If we do so, the probability of emergence of life for $\Lambda \gg \rho_0$ will be additionally suppressed, which will increase the probability to live in an accelerating universe with $0.5 < \Omega_D < 0.9$.

To the best of our knowledge, only in the models based on extended supergravity the relation $|m^2| \sim$ H^2 , together with the absence of freedom to add the bare cosmological constant, is a property of the theory rather than of a particular dynamical regime. That is why the increase of $V(\phi)$ in such models entails the increase in $|m^2|$. This, in its turn, speeds up the development of the cosmological instability, which leads to the anthropically unacceptable consequences.

The N = 8 model discussed in our paper is just a toy model. In this model we were able to find a complete solution to the cosmological constant problem and to the coincidence problem (explaining why $\Lambda \sim \rho_0$ and why Ω_D noticeably differs both from 0 and from 1 at the present stage of the evolution of the universe). This model has important advantages over many other theories of dark energy, but to make it fully realistic one would need to construct a complete theory of all fundamental interactions including the dark energy sector described above. This is a very complicated task that is beyond the scope of the present investigation. However, most of our results are not model-specific. For example, instead of N = 8 supergravity one could study any model with the effective potential of the type $V(\phi) = \Lambda(1 - \alpha\phi^2)$ with $\alpha = O(1)$. Another example is provided by the simplest N=1 Polónyi-type SUGRA model with a very low scale of supersymmetry breaking and with a minimum of the effective potential at $V(\phi) < 0$. As shown in [19], models of this type also have the crucial property $|m^2| \sim H^2$. In fact, this property is required in most of the models of quintessence.

Therefore it would be interesting to apply our methods to the models not necessarily related to extended supergravity. A particularly interesting example is the axion quintessence model. The original model suggested in [24] has the potential $\Lambda[\cos{(\phi/f)} + C]$, and it was assumed that C = 1. It was however emphasized in [24] that this is just an assumption. The positive definiteness of the potential with C = 1 and the fact that it has a minimum at V = 0 could be motivated, in particular, by the global supersymmetry arguments. In supergravity and M/string theory these arguments are no longer valid and the derivation of the value of the parameter C is not available. In [25] the axion model of quintessence was studied using the arguments based on M/string theory. The potential was given in the form $V = \Lambda \cos(\phi/f)$ without any constant part.

This potential has a maximum at $\phi = 0$, $V(0) = \Lambda$. The universe collapses when the field ϕ rolls to the minimum of its potential $V(f\pi) = -\Lambda$. The curvature of the effective potential in its maximum is given by $m^2 = -\Lambda/f^2 = -3H_0^2/f^2$. For $f = M_p = 1$ one finds $m^2 = -\Lambda = -3H_0^2$, and for $f = M_p/\sqrt{2}$ one has $m^2 = -2\Lambda = -6H_0^2$, exactly as in the N = 8 supergravity. Therefore the anthropic constraints on Λ based on the investigation of the collapse of the universe in this model (for C = 0) are similar to the constraints obtained in our paper for the N = 8 theory [26]. However, in this model, unlike in the models based on extended supergravity, one can easily add or subtract any value of the cosmological constant. In order to obtain useful anthropic constraints on the

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7

cosmological constant in this model one should use a combination of our approach with the usual approach based on the theory of galaxy formation [9, 10, 11, 12, 13, 14].

In this sense, our main goal was not to replace the usual anthropic approach to the cosmological constant problem, but to suggest its possible enhancement. We find it very encouraging that our approach may strengthen the existing anthropic constraints on the cosmological constant in the context of the theories based on extended supergravity.

One may find it hard to believe that in order to explain the results of cosmological observations one should consider theories with an unstable vacuum state. However, one should remember that exponential expansion of the universe during inflation, as well as the process of galaxy formation, is the result of the gravitational instability, so we should learn how to live with the idea that our world can be unstable. Also, we did not willingly pick up the theories with an unstable vacuum. We wanted to find the models based on M/string theory that would be capable of describing de Sitter state. All models related to M/string theory that we were able to find so far, with exception of the recently constructed model based on N = 2 supergravity [27], lead to unstable dS vacuum. So maybe we need to take this instability seriously.

This brings us good news and bad news. The bad news is that in all the theories we have considered in this paper, our part of the universe is going to collapse within the next 10-20 billion years or so.

The good news is that we still have a lot of time to find out whether this is really going to happen.

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